

$Dead_{load} := 1.7 \text{ kPa}$ $Live_{load} := 4.8 \text{ kPa}$ $\gamma_{conc} := 23.6 \frac{\text{kN}}{\text{m}^3}$
 not including conc weight

$Dead_{load} + .15 \text{ m} \cdot \gamma_{conc} = 5.24 \text{ kPa}$ $l_w := 4000 \text{ mm}$

SLAB

maximum downward (gravity loads)

ULS factored loads

Given

dead	live	snow	earthquake	wind
$D := 5.24 \text{ kPa}$	$L := 4.8 \text{ kPa}$	$S := 0 \text{ kPa}$	$E := 000 \text{ kPa}$	$W := 000 \text{ kPa}$

step 1

gravity loads are +ve Upward loads are -ve

CASE 1 =	$C_1 := 1.4 \cdot D$	$C_1 = 7.336 \times 10^3 \text{ Pa}$
CASE 2a =	$C_{2a} := (1.25 \cdot D) + (1.5 \cdot L) + 0.5S$	$C_{2a} = 1.375 \times 10^4 \text{ Pa}$
CASE 2b =	$C_{2b} := (1.25 \cdot D) + (1.5 \cdot L) + 0.4W$	$C_{2b} = 1.375 \times 10^4 \text{ Pa}$
CASE 3a =	$C_{3a} := (1.25 \cdot D) + (1.5 \cdot S) + 0.5L$	$C_{3a} = 8.95 \times 10^3 \text{ Pa}$
CASE 3b =	$C_{3b} := (1.25 \cdot D) + (1.5 \cdot S) + 0.4W$	$C_{3b} = 6.55 \times 10^3 \text{ Pa}$
CASE 4a =	$C_{4a} := (1.25 \cdot D) + (1.4 \cdot W) + 0.5L$	$C_{4a} = 8.95 \times 10^3 \text{ Pa}$
CASE 4b =	$C_{4b} := (1.25 \cdot D) + (1.4 \cdot W) + 0.5S$	$C_{4b} = 6.55 \times 10^3 \text{ Pa}$

$$\max_{\text{total}} := \max(C_1, C_{2a}, C_{2b}, C_{3a}, C_{3b}, C_{4a}, C_{4b})$$

$$\max_{\text{total}} = 13.75 \cdot \text{kPa}$$

consider 1m section

step 2

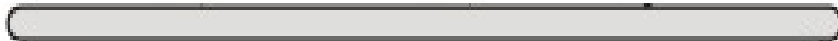
150 = depth 20 = cover 11.3/2 = rebar dia/2

$$M_f := \frac{(\max_{\text{total}} \cdot 1\text{m}) \cdot l^2}{8}$$

$$b := 1000\text{mm} \quad d := 150\text{mm} - 20\text{mm} - \frac{11.3\text{mm}}{2}$$

$$t := 150\text{mm}$$

$$M_f = 27.5 \text{ m} \cdot \text{kN}$$



step 3

$$K_r := \frac{M_f}{b \cdot d^2}$$

$$F_y := 400 \text{ MPa} \quad F_{cprime} := 20 \text{ MPa}$$

$$K_r = 1.778 \cdot \text{MPa} \quad \text{goto excell based on } K_r \text{ now}$$

$$\rho := 0.58\% \quad \text{from excell}$$

step 4

$$A_s := \rho \cdot b \cdot d \quad \text{step 5}$$

$$A_s = 721.23 \cdot \text{mm}^2$$

check for minimim area

$$A_{smin} := 0.002 \cdot (b \cdot t)$$

step 6

slab or footing

$$A_{smin} = 300 \cdot \text{mm}^2$$

$$A_s \geq A_{smin} = 1$$

$$\max_{used} := \max(A_{smin}, A_s)$$

$$\max_{used} = 721.23 \cdot \text{mm}^2 \quad \text{step 7}$$

$$\text{bar}_{number} := \frac{A_s}{100 \text{ mm}}$$

$$\text{bar}_{number} = 7.212 \cdot \text{mm}$$

number of bars

step 8

$$\text{bar}_{spacing} := \frac{b}{7.21}$$

$$\text{bar}_{spacing} = 138.696 \cdot \text{mm}$$

therefore 130mm offset

step 9

$$a_{\max} := 1.4(20\text{mm})$$

$$d_b := 1.4 \cdot 11.3\text{mm}$$

$$\text{dia}_{\text{rebar}} := 1.4 \cdot 11.3\text{mm}$$

$$a_{\max} = 28 \cdot \text{mm}$$

$$d_b = 15.82 \cdot \text{mm}$$

$$\text{dia}_{\text{rebar}} = 15.82 \cdot \text{mm}$$

step 10 = how many bars @ barspacing
with location (bottom/top)

step 11

clear bar spacing minimum

$$\text{bar}_{\text{spacing}} \geq d_b = 1$$

$$\text{bar}_{\text{spacing}} \geq a_{\max} = 1$$

$$\text{bar}_{\text{spacing}} \geq 30\text{mm} = 1$$

step 12

maximum

$$\text{principle}_{\text{spacing}} \leq \left(\frac{3 \cdot t}{500\text{mm}} \right)$$

$$\text{bar}_{\text{spacing}} \leq 3 \cdot t = 1$$

$$\text{bar}_{\text{spacing}} \leq 500\text{mm} = 1$$

Step 13 crack control

$$F_y = 400 \cdot \text{MPa}$$

$$f_c := 0.6 \cdot F_y$$

$$f_c = 240 \cdot \text{MPa}$$

$$A := \frac{\left(20\text{mm} + \frac{11.3\text{mm}}{2} \right) \cdot 2}{\text{bar}_{\text{number}}}$$

$$A = 7.113$$

Question 2 BEAMS

$$\text{Dead}_{\text{load}} := 1.7 \text{ kPa} \quad \text{Live}_{\text{load}} := 4.8 \text{ kPa} \cdot 4 \text{ m} \quad \gamma_{\text{conc}} := 23.6 \frac{\text{kN}}{\text{m}^3} \quad l := 8000 \text{ mm}$$

not including conc weight $\text{Live}_{\text{load}} = 19.2 \cdot \frac{\text{kN}}{\text{m}}$

$$\text{Dead}_{\text{load}} \cdot 4 \text{ m} + [(.15 \text{ m} \cdot 4 \text{ m}) \cdot \gamma_{\text{conc}}] + [0.4 \text{ m} \cdot (.65 \text{ m} - .15 \text{ m}) \cdot \gamma_{\text{conc}}] = 25.68 \cdot \frac{\text{kN}}{\text{m}}$$

dead load

concrete weight

maximum downward (gravity loads)

ULS factored loads

Given

dead	live	snow	earthquake	wind
$D := 25.68 \frac{\text{kN}}{\text{m}}$	$L := 19.2 \frac{\text{kN}}{\text{m}}$	$S := 0 \frac{\text{kN}}{\text{m}}$	$E := 000 \frac{\text{kN}}{\text{m}}$	$W := 000 \frac{\text{kN}}{\text{m}}$

step 1

gravity loads are +ve Upward loads are -ve

CASE 1 =	$C_1 := 1.4 \cdot D$	$C_1 = 3.595 \times 10^4 \frac{\text{kg}}{\text{s}^2}$
CASE 2a =	$C_{2a} := (1.25 \cdot D) + (1.5 \cdot L) + 0.5S$	$C_{2a} = 6.09 \times 10^4 \frac{\text{kg}}{\text{s}^2}$
CASE 2b =	$C_{2b} := (1.25 \cdot D) + (1.5 \cdot L) + 0.4W$	$C_{2b} = 6.09 \times 10^4 \frac{\text{kg}}{\text{s}^2}$
CASE 3a =	$C_{3a} := (1.25 \cdot D) + (1.5 \cdot S) + 0.5L$	$C_{3a} = 4.17 \times 10^4 \frac{\text{kg}}{\text{s}^2}$
CASE 3b =	$C_{3b} := (1.25 \cdot D) + (1.5 \cdot S) + 0.4W$	$C_{3b} = 3.21 \times 10^4 \frac{\text{kg}}{\text{s}^2}$
CASE 4a =	$C_{4a} := (1.25 \cdot D) + (1.4 \cdot W) + 0.5L$	$C_{4a} = 4.17 \times 10^4 \frac{\text{kg}}{\text{s}^2}$
CASE 4b =	$C_{4b} := (1.25 \cdot D) + (1.4 \cdot W) + 0.5S$	$C_{4b} = 3.21 \times 10^4 \frac{\text{kg}}{\text{s}^2}$

$$\text{max}_{\text{total}} := \max(C_1, C_{2a}, C_{2b}, C_{3a}, C_{3b}, C_{4a}, C_{4b})$$

$$\text{max}_{\text{total}} = 60.9 \cdot \frac{\text{kN}}{\text{m}}$$

consider 1m section

step 2

650 = depth 30 = cover 11.3/2 = rebar dia/2

$$M_f := \frac{(\max_{\text{total}}) \cdot 1^2}{8}$$

$$b := 400 \text{ mm}$$

$$d := 650 \text{ mm} - 30 \text{ mm} - 11.3 \text{ mm} - \frac{29.9 \text{ mm}}{2} - 2$$

$$t := 150 \text{ mm} \quad d = 563.79 \text{ mm}$$

$$M_f = 487.2 \text{ m} \cdot \text{kN}$$



step 3

$$K_r := \frac{M_f}{b \cdot d^2}$$

$$F_c := 400 \text{ MPa}$$

$$F_{\text{prime}} := 20 \text{ MPa}$$

$$K_r = 3.832 \text{ MPa} \quad \text{goto excell based on } K_r \text{ now}$$

$$\rho := 1.47\% \quad \text{from excell}$$

step 4

$$A_s := \rho \cdot b \cdot d$$

step 5

$$A_s = 3315.085 \text{ mm}^2$$

$$A_{s\text{min}} := 0.2 \cdot \frac{\sqrt{\frac{F_c}{\text{MPa}} \cdot b \cdot d_1}}{\frac{F_y}{\text{MPa}}}$$

$$F_c := 20 \text{ MPa}$$

$$F_y = 400 \text{ MPa}$$

$$b_t := b \quad d_1 := 650 \text{ mm}$$

$$b = 400 \text{ mm}$$

step 6

for a beam

$$A_{s\text{min}} = 581.378 \text{ mm}^2$$

$$A_s \geq A_{s\text{min}} = 1$$

$$\max_{\text{used}} := \max(A_{s\text{min}}, A_s)$$

$$\max_{\text{used}} = 3315.085 \text{ mm}^2$$

step 7

$$\text{bar_number} := \frac{A_s}{700\text{mm}}$$

divide by area of the bar $A1 = 702.154 \cdot \text{mm}^2$ AREA of bar use ' $\sqrt{}$

$$\text{bar_number} = 4.736 \cdot \text{mm}$$

number of bars **step 8**

$$\text{bar_spacing} := \frac{b}{5}$$

$$\text{bar_spacing} = 80 \cdot \text{mm}$$

therefore 80mm offset **step 9**

$$a_{\text{max}} := 1.4(30\text{mm}) \quad d_b := 1.4 \cdot 11.3\text{mm} \quad \text{dia}_{\text{rebar}} := 1.4 \cdot 11.3\text{mm}$$

$$a_{\text{max}} = 42 \cdot \text{mm} \quad d_b = 15.82 \cdot \text{mm} \quad \text{dia}_{\text{rebar}} = 15.82 \cdot \text{mm}$$

step 10 = how many bars @ barspacing with location (bottom/top)

step 11

clear bar spacing minimum

$$\text{bar_spacing} \geq d_b = 1$$

$$\text{bar_spacing} \geq a_{\text{max}} = 1$$

$$\text{bar_spacing} \geq 30\text{mm} = 1$$

step 12

maximum

$$\text{principle_spacing} \leq \left(\begin{array}{l} 3 \cdot t \\ 500\text{mm} \end{array} \right)$$

$$\text{bar_spacing} \leq 3 \cdot t = 1$$

$$\text{bar_spacing} \leq 500\text{mm} = 1$$

Step 13 crack control

$$F_y = 400 \cdot \text{MPa} \quad f_{\text{max}} := 0.6 \cdot F_y \quad d_c := 30\text{mm} + 11.3\text{mm} + \frac{29.9\text{mm}}{2}$$

$$f_c = 240 \cdot \text{MPa} \quad d_c = 56.25 \cdot \text{mm}$$

y is equal to d.c if one layer if two layer use y

$$y := 30\text{mm} + 11.3\text{mm} + \frac{29.9\text{mm}}{2} + 29.96\text{mm}$$
$$y = 86.21\text{mm}$$

$$A := \frac{2 \cdot y \cdot b}{5}$$

$$A = 13793.6 \cdot \text{mm}^2$$

$$Z := \frac{f_c}{\text{MPa}} \cdot \sqrt[3]{\frac{d_c \cdot A}{\text{mm} \cdot \text{mm}^2}} \cdot 10^{-3}$$

$$Z = 22.054$$

Size	Nominal Diameter (mm)	Mass (kg/m)	Area (mm ²)	Common Uses
10M	11.3	0.785	100	Beam stirrups, column ties, slab/wall/footing longitudinal reinforcing.
15M	16.0	1.570	200	
20M	19.5	2.355	300	Slab/wall/beam/column/footing longitudinal reinforcing.
25M	25.2	3.925	500	
30M	29.9	5.495	700	Beam/column longitudinal reinforcing.
35M	35.7	7.850	1000	
45M	43.7	11.775	1500	Column longitudinal reinforcing.
55M	56.4	56.4	2500	

9.96mm

$$A1 := \frac{\pi \cdot (29.9\text{mm})^2}{4}$$

$$A2 := \frac{\pi \cdot (29.9\text{mm})^2}{4}$$

$$A1 = 702.154 \cdot \text{mm}^2$$

$$A2 = 702.154 \cdot \text{mm}^2$$

$$A1 \cdot 3 = 2106.461 \cdot \text{mm}^2$$

$$A2 \cdot 2 = 1404.308 \cdot \text{mm}^2$$

$$A_{\text{sum}} := (A1 \cdot 3) + (A2 \cdot 2)$$

$$A_y := (A2 \cdot 2) \cdot (29.9\text{mm} + 45\text{mm})$$

$$A_{\text{sum}} = 3.511 \times 10^3 \cdot \text{mm}^2$$

$$A_y = 105182.641 \cdot \text{mm}^3$$

$$Y_c := \frac{A_y}{A_{\text{sum}}}$$

$$Y_c = 29.96 \cdot \text{mm}$$

from center of the bottom bar

value of max for A.s